

Bellwork:

solve: $4(x-1)^2 = 8$

$$\sqrt{(x-1)^2} = \sqrt{2}$$

$$x-1 = \pm\sqrt{2}$$

$$x = 1 \pm \sqrt{2}$$

Chapter 4.6: Perform Operations with Complex Numbers

What is the solution to $x^2 = -1$?

- Not all answers are Real Numbers...
We call these Imaginary numbers, i .

$$i = \sqrt{-1}$$

$$i^2 = -1$$

$$i^3 = -i$$

$$i^4 = 1$$



ex. Solve: $2x^2 + 11 = -37$

$$\frac{2x^2}{2} = \frac{-48}{2}$$

$$\sqrt{x^2} = \sqrt{-24}$$

$$x = \pm \sqrt{+24}i$$

$$x = \pm 2\sqrt{6}i$$

Complex Number System ($a+bi$)

Real Numbers
($a+0i$)

Imaginary Numbers
($0+bi$)

3

$2i$

$3+4i$

Properties:

$$(a + bi) + (c + di) = (a + c) + (b + d)i$$

$$(a + bi) - (c + di) = (a - c) + (b - d)i$$

*Hint... Just add like terms

ex. Simplify:

a. $(8 - i) + (5 + 4i)$

$$8 - i + 5 + 4i$$

$$13 + 3i$$

b. $(7 - 6i) - (3 - 6i)$

$$7 - 6i - 3 + 6i$$

$$4 + 0i$$

c. $10 - (6 + 7i) + 4i$

$$10 - 6 - 7i + 4i$$

$$4 - 3i$$

ex. Write the expression as a complex number in standard form.

$$4i(-6+1)$$

$$-24i + 4i$$

$$= -20i$$

$$0 - 20i$$

$$a + bi$$

$$(9-2i)(-4+7i)$$

$$-36 + 63i + 8i - 14i^2$$

$$-36 + 71i + 14$$

$$-22 + 71i$$

Complex Conjugates....

remember... $5 + \sqrt{2} \longleftrightarrow 5 - \sqrt{2}$

so... $3 + 5i \longleftrightarrow 3 - 5i$

ex. Write in standard form.

$$\frac{(7+5i)(1+4i)}{(1-4i)(1+4i)} = \frac{7+28i+5i+20i^2}{1+16i^2}$$

$$= \frac{-13+33i}{17}$$

$$\boxed{-\frac{13}{17} + \frac{33}{17}i}$$

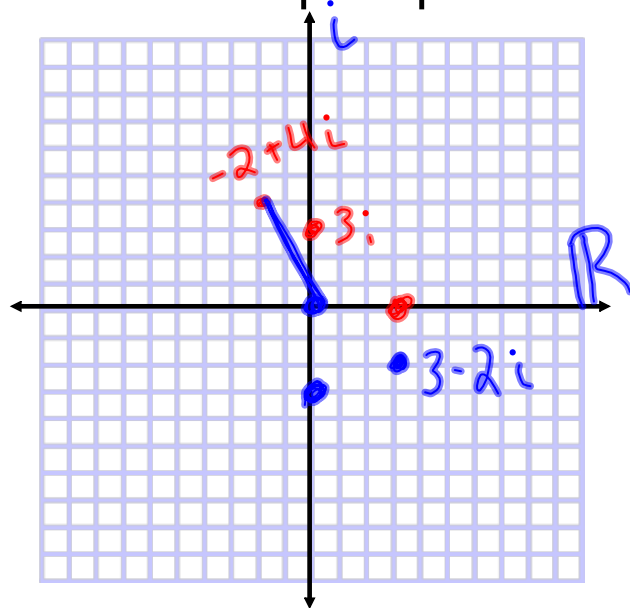
ex. Plot the numbers on the complex plane.

a. $3-2i$

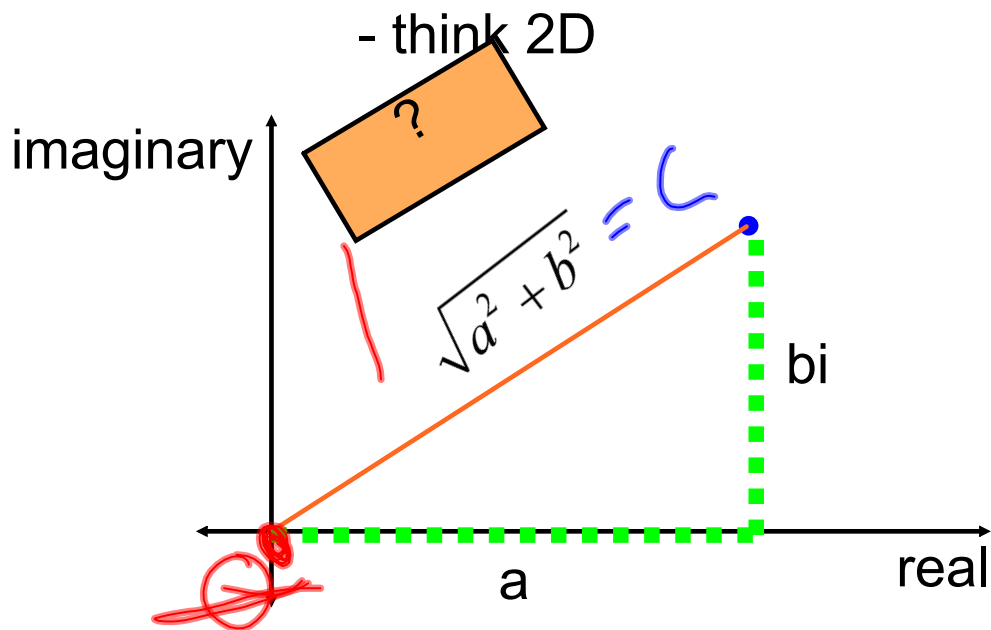
b. $-2+4i$

c. $3i \rightarrow 0+3i$

d. ~~$-4-3i$~~
3



What is the absolute value?



ex. Find the absolute value of:

a. $|-4+3i|$

$$\sqrt{(-4)^2 + (3)^2}$$

$$\sqrt{16 + 9}$$

$$\sqrt{25} = 5$$

b. $-3i$ $0-3i$

$$\sqrt{0^2 + (-3)^2}$$

$$\sqrt{0 + 9}$$

$$\sqrt{9} = 3$$

Homework: Chapter 4.6 pg.279
#'s 4-32e, 42,44,50,54,56,68